



Pearson
Edexcel

Mark Scheme (Results)

October 2020

Pearson Edexcel IAL In Statistics 1
Paper WST03/01

| Question Number | Scheme | Marks |
|-----------------|---|----------------|
| 1. | | |
| (a) | $E(2\bar{X}) = 2E(\bar{X}) = \frac{2(1+\alpha)}{2}$ | M1 |
| | $= 1 + \alpha \neq \alpha$ (therefore $2\bar{X}$ is a biased estimator of α) | A1 |
| | | (2) |
| (b) | $\bar{x} = 6 \quad 2\bar{x} - 1 =$ | M1 |
| | <u>11</u> | A1 |
| | | (2) |
| | | Total 4 |
| | Notes | |
| (a) | M1 for use of $2 \times \frac{1+\alpha}{2}$ Also correct comparison with α and no incorrect working seen. $\frac{1+\alpha}{2} \neq \alpha$ is M0A0 | |
| (b) | M1 for attempt at \bar{x} and use of $2\bar{x} - 1$ or ft use of their $E(\bar{X})$ from part (a) to find an estimate for α A1 11 cao | |

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|-----------------|--|-------|------|------|------|------|--|--|--|--|--|------|----|--|
| 2. (a) | Expected values: 13.75, 19.25, 17 | B1 | | | | | | | | | | | | |
| | $\frac{(18-13.75)^2}{13.75} \quad \frac{(15-19.25)^2}{19.25} \quad \frac{(17-17)^2}{17}$ | M1 | | | | | | | | | | | | |
| | <table border="1"> <tr> <td>Pass</td> <td>1.31</td> <td>0.94</td> <td>0</td> <td>2.25</td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>9.43</td> <td>A2</td> </tr> </table> | Pass | 1.31 | 0.94 | 0 | 2.25 | | | | | | 9.43 | A2 | |
| | Pass | 1.31 | 0.94 | 0 | 2.25 | | | | | | | | | |
| | | | | | 9.43 | A2 | | | | | | | | |
| | | (4) | | | | | | | | | | | | |
| | | | | | | | | | | | | | | |
| (b) | H_0 : <u>Degree/category</u> is independent of <u>department</u> (no association) H_1 : Degree/category is not independent of department (association) | B1 | | | | | | | | | | | | |
| | $\nu = (3-1)(3-1) = 4$ | B1 | | | | | | | | | | | | |
| | $\chi_4^2(5\%) = 9.488$ | B1ft | | | | | | | | | | | | |
| | '9.43' < 9.488, so do not reject H_0 / not significant | M1 | | | | | | | | | | | | |
| | Not enough evidence to show that the Degree/category is not independent of department (no association) (at the 5% level of significance) | A1ft | | | | | | | | | | | | |
| | | (5) | | | | | | | | | | | | |
| | Total 9 | | | | | | | | | | | | | |
| | Notes | | | | | | | | | | | | | |
| (a) | B1 All correct expected values (may be implied by A2) M1 Attempting $\frac{(O-E)^2}{E}$ for their E (may be implied by one correct value) A2 all 5 values correct (allow awrt) (A1 any 2 values correct) | | | | | | | | | | | | | |
| (b) | B1 Both hypotheses required must mention degree/category and department at least once. Use of "relationship" or "correlation" or "connection" or "link" award B0. B1 4 can be implied by 9.488 seen B1ft 9.488 or better. Follow through their ν so may see $\chi_{3,0.05}^2 = 7.815$ $\chi_{2,0.05}^2 = 5.991$ M1 Correct non-contextual conclusion for their (a) and c.v. Can be implied by correct conclusion in context ft their (a) and c.v. A1ft A correct comment in context. Condone "relationship" or "connection" here but not "correlation". Follow through from their test statistic and cv, but hypotheses must be correct. | | | | | | | | | | | | | |

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|-----------------|---|-----------------|------|------|-----|-------|-----|---|---|---|---|-----|---|---|---|---|-----|---|---|----|---|-----|---|---|----|---|-----|---|---|---|---|-----|---|---|---|---|-----|---|---|---|---|-------|
| 3. | <table border="1"> <thead> <tr> <th></th> <th>200m</th> <th>400m</th> <th>d</th> <th>d^2</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>3</td> <td>1</td> <td>2</td> <td>4</td> </tr> <tr> <td>B</td> <td>2</td> <td>2</td> <td>0</td> <td>0</td> </tr> <tr> <td>C</td> <td>1</td> <td>4</td> <td>-3</td> <td>9</td> </tr> <tr> <td>D</td> <td>4</td> <td>5</td> <td>-1</td> <td>1</td> </tr> <tr> <td>E</td> <td>7</td> <td>7</td> <td>0</td> <td>0</td> </tr> <tr> <td>F</td> <td>6</td> <td>6</td> <td>0</td> <td>0</td> </tr> <tr> <td>G</td> <td>5</td> <td>3</td> <td>2</td> <td>4</td> </tr> </tbody> </table> | | 200m | 400m | d | d^2 | A | 3 | 1 | 2 | 4 | B | 2 | 2 | 0 | 0 | C | 1 | 4 | -3 | 9 | D | 4 | 5 | -1 | 1 | E | 7 | 7 | 0 | 0 | F | 6 | 6 | 0 | 0 | G | 5 | 3 | 2 | 4 | M1 A1 |
| | | | 200m | 400m | d | d^2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | A | 3 | 1 | 2 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | B | 2 | 2 | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | C | 1 | 4 | -3 | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| D | 4 | 5 | -1 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| E | 7 | 7 | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| F | 6 | 6 | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| G | 5 | 3 | 2 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (a) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | $\sum d^2 = 18$ | A1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | $r_s = 1 - \frac{6 \times 18}{7 \times 48} = \frac{19}{28} = \text{awrt } \underline{0.679}$ | dM1 A1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | (5) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (b) | $H_0 : \rho = 0$ $H_1 : \rho > 0$ | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Critical value 0.7143 | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | (0.679 < 0.7143) so insufficient evidence to reject H_0 | M1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | There is insufficient evidence to suggest a positive correlation between the finishing order in the 200 metre race and the finishing order in the 400 metre race. | A1ft | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | (4) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (c) | There are tied lengths so use average ranks | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Then use $r_s = \frac{S_{xy}}{\sqrt{S_{xx}S_{yy}}}$ | dB1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | (2) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | Total 11 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Notes | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (a) | M1 for an attempt to rank athletes lists (at least 3 correct for each) A1 for correct rankings for both (may be reversed). Can be implied by correct $\sum d^2$ A1 $\sum d^2 = 18$ dM1 (dep upon previous M1) for use of the correct formula, follow through their $\sum d^2$ A1 awrt 0.679 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (b) | B1 both hypotheses correct ρ or ρ_s B1 for correct c.v. (sign should match H_1 or r_s) M1 ft their r_s and their c.v. A1 ft a correct contextualised comment including positive correlation and races/finishing orders (oe) with all previous marks in (b) scored | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (c) | B1 for use of average ranks or use of 1.5 or 6.5 (for C and D)/4.5 or 3.5 (for B and G) dB1 (dep on 1 st B1) for use of pmcc (with the average ranks) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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|--|---|-----------------|---------------------|---------------------|-----------------|----|----|-------|--------|----|----|-------|--------|----|----|-----|------|----|----|-----|------|----|----|-----|------|-----|-----|------|--------|-------------|
| 4. (a) | Randomly select a student from 1 to 7 oe | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Take every 7 th student | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | (2) | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (b) | $\nu = 10 - 1 = 9$ $\chi_9^2(10\%) = 14.684$ | B1 B1ft | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | No evidence (at 10% level of significance) that the digits generated do not follow a uniform distribution . | dB1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | (3) | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (c) | H_0 : Uniform distribution is a good fit (for the two-digit numbers generated) H_1 : Uniform distribution is not a good fit (for the two-digit numbers generated) | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | <table border="1"> <thead> <tr> <th>O</th> <th>E</th> <th>$\frac{(O-E)^2}{E}$</th> <th>$\frac{O^2}{E}$</th> </tr> </thead> <tbody> <tr> <td>31</td> <td>40</td> <td>2.025</td> <td>24.025</td> </tr> <tr> <td>49</td> <td>40</td> <td>2.025</td> <td>60.025</td> </tr> <tr> <td>30</td> <td>40</td> <td>2.5</td> <td>22.5</td> </tr> <tr> <td>42</td> <td>40</td> <td>0.1</td> <td>44.1</td> </tr> <tr> <td>48</td> <td>40</td> <td>1.6</td> <td>57.6</td> </tr> <tr> <td>200</td> <td>200</td> <td>8.25</td> <td>208.25</td> </tr> </tbody> </table> | O | E | $\frac{(O-E)^2}{E}$ | $\frac{O^2}{E}$ | 31 | 40 | 2.025 | 24.025 | 49 | 40 | 2.025 | 60.025 | 30 | 40 | 2.5 | 22.5 | 42 | 40 | 0.1 | 44.1 | 48 | 40 | 1.6 | 57.6 | 200 | 200 | 8.25 | 208.25 | B1 M1 A1 |
| | O | E | $\frac{(O-E)^2}{E}$ | $\frac{O^2}{E}$ | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 31 | 40 | 2.025 | 24.025 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 49 | 40 | 2.025 | 60.025 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 30 | 40 | 2.5 | 22.5 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 42 | 40 | 0.1 | 44.1 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 48 | 40 | 1.6 | 57.6 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 200 | 200 | 8.25 | 208.25 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\sum \frac{(O-E)^2}{E} = 8.25$ or $\sum \frac{O^2}{E} - 200 = 8.25$ | A1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\chi_4^2(10\%) = 7.779$ | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| [8.25 > 7.779] Reject H_0 / Significant | M1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| There is evidence to suggest the two-digit numbers generated may not follow a uniform distribution . | A1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | (8) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (d) | To generate a simple random sample, Luka would need to generate two-digit numbers (from 00 to 69) | B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | But Luka's table would not be suitable for generating random two-digit numbers | B1ft | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | (2) | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | Total 15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Notes | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (a) | B1 for the idea of generating a random number to determine first student selected | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (b) | B1 for every 7th student (not just select 40 students) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | B1ft for correct degrees of freedom (may be implied by 2 nd B1) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | B1ft for correct critical value 14.684 or better ft their d.f. so may see $\chi_{10}^2(10\%) = 15.987$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (c) | B1 (dependent upon 2 nd B1) for correct conclusion in context with digits (oe) and uniform distr. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | B1 Both hypotheses correct | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | B1 All expected values = 40 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | M1 Attempting $\frac{(O-E)^2}{E}$ or $\frac{O^2}{E}$ with at least 3 correct (1 dp truncated or rounded) or f.t. their E | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | A1 all $\frac{(O-E)^2}{E}$ or $\frac{O^2}{E}$ correct (1 dp truncated or rounded). May be implied by 8.25 or 208.25 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | A1 8.25 oe | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | B1 correct critical value 7.779 or better | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | M1 for a correct non-contextual conclusion (ignore any contradictory contextual comments for this mark) based on their cv and their test statistic | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | A1 correct conclusion in context with all previous marks scored | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (d) | B1 for the idea of generating two-digit numbers (for a simple random sample) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | B1ft Luka's table not suitable for generating two-digit random numbers for a simple random sample, ft parts (b) and (c) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| SC: | If B0B0 scored, 'table only suitable for generating one-digit random numbers' scores B0B1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Question Number | Scheme | Marks |
|-----------------|---|---|
| 5. | | |
| (a) | $s_A^2 = \frac{1}{39}(790258 - 140.4^2 \times 40)$ $s_B^2 = \frac{1}{31}(581430 - 134.7^2 \times 32)$ $= 45.4256\dots$ awrt 45.4 $= 26.4232\dots$ awrt 26.4 | M1 A1 A1 (3) |
| (b) | $H_0 : \mu_A - \mu_B = 5$ $H_1 : \mu_A - \mu_B > 5$ $s.e. = \sqrt{\frac{45.4256\dots}{40} + \frac{26.4232\dots}{32}}$ (= awrt 1.4) $z = \frac{\pm(140.4 - 134.7 - 5)}{s.e.}$ = awrt 0.50 c.v. = 1.6449 (Do not reject H_0) Insufficient evidence to support the greengrocer's belief . (Insufficient evidence that the difference in weight between type A oranges and type B oranges is over 5 grams). | B1 B1 M1 dM1 A1 B1 A1ft (7) |
| (c) | Large sample sizes so... Sample means are normally distributed (CLT) $s_A^2 = \sigma_A^2$ and $s_B^2 = \sigma_B^2$ | B1 B1 (2) |
| | | Total 12 |
| | Notes | |
| (a) | M1 one correct expression A1 either awrt 45.4 or awrt 26.4 A1 both awrt 45.4 and awrt 26.4 | |
| (b) | B1 Allow equivalent rearrangements. Must use μ B1 Allow equivalent rearrangements. Must use μ . For both hypotheses do not allow e.g. μ_1 and μ_2 unless each has been clearly defined M1 attempt at standard error (allow one slip) ft their (a) dM1 standardising with $(140.4 - 134.7 - 5)$ and their s.e. (dep on previous M1) A1 for 0.5 or awrt 0.50 B1 correct c.v. 1.6449 or better. Allow -1.6449 or better with use of $\mu_B - \mu_A$ Allow $p = \text{awrt } 0.309$ A1ft correct ft conclusion in context with either greengrocer's belief (oe) or difference in weights (oe) dependent on all B and M marks scored. | |
| (c) | B1 must comment on both sample means, \bar{A} and \bar{B} B1 must comment on both variances/standard deviations | |

| Question Number | Scheme | Marks |
|-----------------|---|----------------|
| 6. | | |
| (a) | $\bar{T} \sim N(4, \frac{4}{35})$ | M1 A1 |
| | | (2) |
| (b) | $\bar{K} \sim N(\lambda, \frac{\lambda}{40})$ | M1 |
| | $2 \times 2.5758 \times \sqrt{\frac{\lambda}{40}} = 2.6$ | B1 M1 |
| | $\lambda = \text{awrt } \underline{10.2}$ | A1 |
| | | (4) |
| (c) | $2 \times 0.99 \times 0.01$ | M1 |
| | $= \underline{0.0198}$ | A1 |
| | | (2) |
| | | Total 8 |
| | Notes | |
| (a) | M1 for Normal distribution A1 for correct mean and variance (allow N(4, awrt 0.114)) | |
| (b) | M1 for use of $\frac{\lambda}{40}$ if $\lambda = \sigma$ is used, then M0 B1 for ± 2.5758 (may be implied by sight of 10.188...) M1 for use of $2 \times z \times \frac{\sigma}{\sqrt{40}} = 2.6$ with $ z > 2$ A1 awrt 10.2 (an answer of 10.15...or awrt 10.2 on its own scores M1B0M1A1) | |
| | SC: Use of $\sqrt{\lambda}$ instead of λ leading to an answer of awrt 3.19... scores M0B1M1A0 | |
| (c) | M1 for $2p(1-p)$ for any p $0 < p < 1$ A1 0.0198 | |

| Question Number | Scheme | Marks |
|-----------------|---|-----------------|
| 7. (a) | $C_1 + C_2 + C_3 \sim N(480, 3 \times 1.25^2)$ | M1 A1 |
| | $P(C_1 + C_2 + C_3 > 475.8) = P\left(Z > \frac{475.8 - 480}{\sqrt{3 \times 1.25^2}} (= -1.94)\right)$ | M1 |
| | = awrt 0.974 | A1 |
| | | (4) |
| (b) | $W = T_1 + T_2 + T_3 + T_4 + T_5 + C_1 + C_2 \sim N(5 \times 60 + 2 \times 160, 5 \times 2^2 + 2 \times 1.25^2)$ | M1 A1 |
| | $P(W > 625) = P\left(Z > \frac{625 - 620}{\sqrt{23.125}} (= 1.03975\dots)\right)$ | M1 |
| | = awrt 0.149 | A1 |
| | | (4) |
| (c) | $Y = (n-1)T_1 - \sum_{r=2}^n T_r$ | |
| | $Y \sim N(\mu, \sigma^2)$ | |
| | $\mu = (n-1) \times 60 - (n-1) \times 60 [= 0]$ | M1 A1 |
| | $\sigma^2 = (n-1)^2 \times 4 + (n-1) \times 4 [= 4n^2 - 4n]$ | M1 A1 |
| | $\frac{40 - 0}{\sqrt{4n^2 - 4n}} = 1.38$ | M1 B1 |
| | $4n^2 - 4n - 840 (.159\dots) = 0$ | dM1 |
| | $n = 15$ | A1 |
| | | (8) |
| Notes | | Total 16 |
| (a) | M1 for setting up Normal distribution with mean 480 A1 for correct expression for variance (= 4.6875) or for standard deviation (= 2.165...) M1 standardising with 475.8, 480 and their standard deviation (their standard deviation \neq 3.75) A1 awrt 0.974 | |
| (b) | M1 for setting up Normal distribution with mean 620 A1 for correct expression for variance (= 23.125) or for standard deviation (= 4.8088...) M1 standardising with 625, 620 and their standard deviation A1 awrt 0.149 | |
| (c) | M1 for a single combined normal distribution (may be implied by a single standardisation) A1 correct expression for μ M1 for use of $a^2 \times 4 + a \times 4$ A1 correct expression for σ^2 M1 standardising with their mean and their sd = z where $1 < z < 1.5$ B1 awrt 1.38 dM1 solving their 3TQ (working must be shown if answer is incorrect) (dependent upon 2 nd M1) A1 15 cao (must reject -14 if found). Must come from compatible signs in standardisation. | |